MATH 300-0 Foundations of Higher Mathematics (1 Unit)
Introduction to fundamental mathematical structures, including sets, functions, equivalence relations, and cardinal numbers. Elementary logic and proof techniques. Students may not receive credit for MATH 300-0 after passing any of MATH 320-1, MATH 321-1, MATH 330-1, or MATH 331-1.
Prerequisite: MATH 240-0 or MATH 281-3 or MATH 285-1 or MATH 290-1 or MATH 291-1 or GEN_ENG 205-1 or GEN_ENG 206-1 or consent of the department.

MATH 300-BR Foundations of Higher Mathematics (1 Unit)
For participants in the Causeway Postbaccalaureate Program only. Introduction to fundamental mathematical structures, including sets, functions, equivalence relations, and cardinal numbers. Elementary logic and proof techniques. Additional topics selected by the instructor.

MATH 306-0 Combinatorics & Discrete Mathematics (1 Unit)
Discrete mathematics, inductive reasoning, counting problems, binomial coefficients and Pascal’s triangle, Fibonacci numbers, set and integer partitions, and generating functions.
Prerequisite: MATH 240-0 or MATH 281-3 or MATH 285-1 or MATH 290-1 or MATH 291-1 or GEN_ENG 205-1 or GEN_ENG 206-1.

MATH 308-0 Graph Theory (1 Unit)
Introduction to graph theory: graphs, trees, matchings, planar graphs, and colorings. Additional topics as time permits.
Prerequisite: MATH 291-1 or MATH 300-0 or MATH 306-0.

MATH 310-1 Probability and Stochastic Processes (1 Unit)
Axioms of probability. Conditional probability and independence. Random variables. Joint distributions. Expectation. Limit theorems: the weak law of large numbers and the central limit theorem. Students may not receive credit for both MATH 310-1 and any of MATH 311-1, MATH 314-0, MATH 385-0, STAT 320-1, STAT 383-0, IEMS 202-0, or ELEC_ENG 302-0.
Prerequisite or corequisite: MATH 226-0 or MATH 281-2; and MATH 228-2 or MATH 230-2 or MATH 234-0 (former), or MATH 281-2 or MATH 285-3 or MATH 290-3 or MATH 291-3 or ES_APPM 252-2.

MATH 310-2 Probability and Stochastic Processes (1 Unit)
Discrete-time Markov chains, recurrence and transience. Students may not receive credit for both MATH 310-2 and MATH 311-2.
Prerequisites: MATH 240-0 or MATH 281-3 or MATH 285-1 or MATH 290-1 or MATH 291-1 or GEN_ENG 205-1 or GEN_ENG 206-1; and MATH 310-1 or MATH 311-1 or MATH 314-0 or MATH 385-0 or STAT 320-1 or STAT 383-0 or IEMS 202-0 or ELEC_ENG 302-0.

MATH 310-3 Probability and Stochastic Processes (1 Unit)
Continuous-time Markov chains, queues, population growth models. Brownian motion and other diffusion processes. Additional topics as time permits. Students may not receive credit for both MATH 310-3 and MATH 311-3.
Prerequisite: MATH 310-2 or MATH 311-2.

MATH 311-1 MENU: Probability and Stochastic Processes (1 Unit)
Probability spaces. Random variables. Independence. Distributions. Generating functions. The central limit theorem. Students may not receive credit for both MATH 311-1 and any of MATH 310-1, MATH 314-0, MATH 385-0, STAT 320-1, STAT 383-0, IEMS 202-0, or ELEC_ENG 302-0.
Prerequisite: MATH 226-0 or MATH 281-2; and MATH 311-3, or MATH 310-2 and any one of MATH 290-3, MATH 281-2, MATH 285-3 or ES_APPM 252-2; or consent of the department. Recommended: MATH 320-1 or MATH 321-1.

MATH 311-2 MENU: Probability and Stochastic Processes (1 Unit)
Markov chains, convergence of random variables, random processes, renewals, and queues. Students may not receive credit for both MATH 311-2 and MATH 310-2.
Prerequisite: MATH 311-1 or consent of the department.

MATH 311-3 MENU: Probability and Stochastic Processes (1 Unit)
Stationary processes, martingales, and diffusion processes. Students may not receive credit for both MATH 311-3 and MATH 310-3.
Prerequisite: MATH 311-2 or consent of the department.

MATH 314-0 Probability and Statistics for Econometrics (1 Unit)
Introduction to probability theory and statistical methods, including properties of probability distributions, sampling distributions, estimation, confidence intervals and hypothesis testing. For students planning to take ECON 381-1. Students may not receive credit for both MATH 314-0 and any of MATH 310-1, MATH 311-1, MATH 385-0, STAT 320-1, STAT 383-0, IEMS 202-0, or ELEC_ENG 302-0.
Prerequisite or corequisite: MATH 226-0 or MATH 281-2; and MATH 228-2 or MATH 230-2 or MATH 234-0 (former) or MATH 281-1 or MATH 285-3 or MATH 290-3 or MATH 291-3 or ES_APPM 252-2.

MATH 320-1 Real Analysis (1 Unit)
Analysis on the real line: axiomatic development of the real number system, sequences and series of real numbers, continuity, and differentiability. Students may not receive credit for both MATH 320-1 and MATH 321-1.
Prerequisite: MATH 226-0 or MATH 281-2; and MATH 300-0 or MATH 291-3; or consent of the department.

MATH 320-2 Real Analysis (1 Unit)
Analysis on the real line: the Riemann integral and sequences and series of functions. Additional topics as time permits. Students may not receive credit for both MATH 320-2 and MATH 321-2.
Prerequisite: MATH 320-1 or MATH 321-1.

MATH 320-3 Real Analysis (1 Unit)
Analysis on Euclidean spaces: the topology of Euclidean spaces, limits, continuity, and differentiability, including the inverse and implicit function theorems. Additional topics as time permits. Students may not receive credit for both MATH 320-3 and MATH 321-2.
Prerequisite: MATH 320-2.

MATH 321-1 MENU: Real Analysis (1 Unit)
Analysis on metric spaces: the real number system, the topology of metric spaces, sequences and series, continuity, and differentiability. Students may not receive credit for both MATH 321-1 and MATH 320-1.
Prerequisite: consent of the department.

MATH 321-2 MENU: Real Analysis (1 Unit)
Analysis on metric spaces: the Riemann integral, sequences and series of functions, and functions of several variables, including the inverse...
and implicit function theorems. Students may not receive credit for both MATH 321-2 and either MATH 320-2 or MATH 320-3.
Prerequisite: MATH 321-1.

**MATH 321-3 MENU: Real Analysis (1 Unit)**
Lebesgue measure and the Lebesgue integral. Additional topics as time permits.
Prerequisite: MATH 321-2.

**Formal Studies Distro Area**

**MATH 325-0 Complex Analysis (1 Unit)**
Complex numbers. Analytic functions. Cauchy's theorem and the Cauchy integral formula. Series. Residues. Students may not receive credit for both MATH 325-0 and either MATH 382-0 or ES_APPM 312-0.
Prerequisites: MATH 226-0 or MATH 281-2; and MATH 228-2 or MATH 230-2 or MATH 234-0 (former) or MATH 281-2 or MATH 285-3 or MATH 290-3 or MATH 291-3 or ES_APPM 252-2; and MATH 240-0 or MATH 281-3 or MATH 285-1 or MATH 290-1 or MATH 291-1 or GEN_ENG 205-1 or GEN_ENG 206-1.

**Formal Studies Distro Area**

**MATH 327-0 Mechanics for Mathematicians (1 Unit)**
Fundamental mathematical ideas arising in classical mechanics: Newtonian mechanics, Lagrangian formalism and the calculus of variations, motion with constraints, symmetries and conservation laws, Hamiltonian mechanics, and Liouville's theorem. No prior knowledge of physics required. Students may not receive credit for MATH 327-0 after taking PHYSICS 330-1.
Prerequisites: MATH 226-0 or MATH 281-2; and MATH 228-2 or MATH 230-2 or MATH 234-0 (former) or MATH 281-2 or MATH 285-3 or MATH 290-3 or MATH 291-3 or ES_APPM 252-2; and MATH 240-0 or MATH 281-3 or MATH 285-1 or MATH 290-1 or MATH 291-1 or GEN_ENG 205-1 or GEN_ENG 206-1.

**Formal Studies Distro Area Interdisciplinary Distro - See Rules (https://catalogs.northwestern.edu/undergraduate/arts-sciences/#schoolrequirementstext)**

**MATH 330-1 Abstract Algebra (1 Unit)**
Group theory. Students may not receive credit for both MATH 330-1 and MATH 331-1.
Prerequisite: MATH 291-1 or MATH 300-0.

**Formal Studies Distro Area**

**MATH 330-2 Abstract Algebra (1 Unit)**
Ring theory, including polynomial rings. Students may not receive credit for both MATH 330-2 and MATH 331-2.
Prerequisite: MATH 330-1 or MATH 331-1.

**Formal Studies Distro Area**

**MATH 330-3 Abstract Algebra (1 Unit)**
Field theory and Galois theory. Students may not receive credit for both MATH 330-3 and MATH 331-3.
Prerequisite: MATH 330-2 or MATH 331-2.

**Formal Studies Distro Area**

**MATH 331-1 MENU: Abstract Algebra (1 Unit)**
Group theory, including the Sylow theorems. Students may not receive credit for both MATH 331-1 and MATH 330-1.
Prerequisite: consent of the department.

**Formal Studies Distro Area**

**MATH 331-2 MENU: Abstract Algebra (1 Unit)**
Ring theory, including polynomial rings. Module theory, including canonical forms of operators on vector spaces. Students may not receive credit for both MATH 331-2 and MATH 330-2.
Prerequisite: MATH 331-1.
and chaos. Students may not receive credit for both MATH 353-0 and MATH 360-2.
Prerequisite: MATH 226-0 or MATH 281-2; and MATH 290-3 or MATH 291-3.

MATH 360-1 MENU: Applied Analysis (1 Unit)
Linear ordinary differential equations, systems of linear ordinary differential equations, and applications. Students may not receive credit for both MATH 360-1 and any of MATH 250-0, MATH 281-3, GEN_ENG 205-4, or GEN_ENG 206-4.
Prerequisite: MATH 226-0 or MATH 281-2; and MATH 290-3 or MATH 291-3.

MATH 360-2 MENU: Applied Analysis (1 Unit)
Qualitative analysis of systems of ordinary differential equations. Linear partial differential equations. Fourier series and orthogonal functions. Applications. Students may not receive credit for both MATH 360-2 and any of MATH 381-0, MATH 351-0, or ES_APPM 311-2.
Prerequisite: MATH 360-1.

MATH 368-0 Introduction to Optimization (1 Unit)
Methods and concepts of optimization theory: linear programming, duality, convexity, and Kuhn-Tucker theory.
Prerequisites: MATH 226-0 or MATH 281-2; and MATH 291-3, or MATH 300-0 and one of MATH 288-2, MATH 230-2, MATH 234-0 (former), MATH 281-2, MATH 285-3, MATH 290-3, or ES_APPM 252-2.

MATH 370-0 Mathematical Logic (1 Unit)
Mathematical formulation and rigorous discussion of logical systems, particularly the propositional calculus and the functional calculi of first and second order. Well-formed formulae, formal languages, proofs, tautologies, effective procedures, deduction theorems, axiom schemata.
Prerequisite: MATH 300-0 or MATH 291-3 or consent of the instructor.

MATH 410-1 Analysis (1 Unit)

MATH 410-2 Analysis (1 Unit)

MATH 410-3 Introduction to Modern Analysis (1 Unit)
Complex analysis. Holomorphic functions, Cauchy’s theorem, power series, harmonic functions, conformal mapping, analytic continuation.

MATH 413-1 Functions of a Complex Variable (1 Unit)
Holomorphic functions: theorems of Cauchy, Morera, and Rouché residue and open mapping theorems; harmonic and entire functions; analytic continuation; conformal mapping. Schlicht functions, functions of several complex variables, Hp spaces, and complex manifolds.

MATH 414-0 Abstract Riemann Surfaces (1 Unit)

MATH 415-1 Functional Analysis (1 Unit)
Topological groups and topological vector spaces; Banach spaces, linear functionals, and operators; applications to functional equations.

MATH 415-2 Functional Analysis (1 Unit)
Topological groups and topological vector spaces; Banach spaces, linear functionals, and operators; applications to functional equations.

MATH 420-1 Partial Differential Equations (1 Unit)
Introduction to basic differential equations, with emphasis on the theory of partial differential equations.
Prerequisites: Advanced calculus and linear algebra or permission of instructor.

MATH 420-2 Partial Differential Equations (1 Unit)
Introduction to basic differential equations, with emphasis on the theory of partial differential equations.
Prerequisites: Advanced calculus and linear algebra or permission of instructor.

MATH 420-3 Partial Differential Equations (1 Unit)
Introduction to basic differential equations, with emphasis on the theory of partial differential equations.
Prerequisites: Advanced calculus and linear algebra or permission of instructor.

MATH 425-1 Partial Differential Equations II (1 Unit)
Nonlinear elliptic differential equations, nonlinear hyperbolic differential equations, pseudodifferential operators, and other topics.

MATH 425-2 Partial Differential Equations II (1 Unit)
Nonlinear elliptic differential equations, nonlinear hyperbolic differential equations, pseudodifferential operators, and other topics.

MATH 425-3 Partial Differential Equations II (1 Unit)
Nonlinear elliptic differential equations, nonlinear hyperbolic differential equations, pseudodifferential operators, and other topics.

MATH 428-0 Geometric Measure Theory & Applications (1 Unit)
General measure theory, Hausdorff measure, area and co-area formulas, Sobolev functions, BV functions and set of finite perimeter, Gauss-Green theorem, differentiability and approximation, applications.

MATH 429-0 Fourier Analysis (1 Unit)
A short overview of classical Fourier analysis on the circle. Selected topics about Fourier analysis on the line and in Euclidean space.
Prerequisite: Permission of instructor.

MATH 430-1 Dynamical Systems (1 Unit)
Qualitative theory of differentiable dynamical systems, emphasizing global properties such as structural stability theorems.

MATH 430-2 Dynamical Systems (1 Unit)
Qualitative theory of differentiable dynamical systems, emphasizing global properties such as structural stability theorems.

MATH 430-3 Dynamical Systems (1 Unit)
Qualitative theory of differentiable dynamical systems, emphasizing global properties such as structural stability theorems.

MATH 435-0 Ergodic Theory (1 Unit)
Introduction to abstract ergodic theory, focusing on the asymptotic behavior of measure preserving transformations. Topics to be covered include: measure preserving transformations and flows, convergence theorems, recurrence properties, isomorphism invariants, and applications to problems in number theory, probability, and combinatorics.
Prerequisite: MATH 410-1.

MATH 438-3 Interdisciplinary Nonlinear Dynamics (1 Unit)
First quarter: Example-oriented survey of nonlinear dynamical systems, including chaos, combining numerical, analytical and geometrical approaches to differential chaos, combining numerical, analytical and geometrical approaches to differential equations. Second and third
MATH 440-1 Geometry and Topology (1 Unit)

MATH 440-2 Geometry and Topology (1 Unit)
Algebraic topology. The fundamental group, covering spaces, and the Van-Kampen theorem. Singular homology, Mayer-Vietoris, degree and Euler characteristic.

MATH 440-3 Geometry and Topology (1 Unit)
de Rham cohomology, Mayer-Vietoris, Poincare’ duality, singular homology and cohomology. Cohomology of cell complexes, simplicial cohomology, Cech cohomology. Cup product; sheaves. Prerequisite: MATH 440-2.

MATH 444-0 Hamiltonian Dynamics and Symplectic Geometry (1 Unit)

MATH 445-1 Differential Geometry (1 Unit)
Riemannian geometry: connections, geodesics, completeness, Jacobi fields, exponential map, constant curvature.

MATH 445-2 Differential Geometry (1 Unit)
Hodge theory: connections, curvature, de Rham complex, Hodge decomposition, Kahler manifolds, Chern-Weil theorem.

MATH 445-3 Differential Geometry (1 Unit)
Further topics: connections and curvature on principal and associated bundles; symplectic geometry, classical mechanics and geometric quantization; Dirac operators and index theorems.

MATH 450-1 Probability Theory & Stochastic Analysis (1 Unit)

MATH 450-2 Probability Theory and Stochastic Analysis (1 Unit)
Random walk, Markov chains, martingales, and stochastic processes. Definition and properties of standard Brownian motion.

MATH 450-3 Probability Theory and Stochastic Analysis (1 Unit)
Stochastic Integration and stochastic differential calculus, with applications to diffusion processes.

MATH 460-1 Algebraic Topology (1 Unit)
Fundamental group and covering spaces.

MATH 460-2 Algebraic Topology (1 Unit)
Simplicial, singular, and cellular (co-) homology; universal coefficient and Kunneth theorems. Prerequisite: MATH 460-1.

MATH 460-3 Algebraic Topology (1 Unit)
Cohomology rings and Poincare duality; Thom Isomorphism and characteristic classes. Prerequisite: MATH 460-2.

MATH 465-1 Algebraic Topology II (1 Unit)
Cohomology theories and operations, homotopy and obstruction theory, and CW complexes; spectral sequences. Multiple registrations allowed.

MATH 465-2 Algebraic Topology II (1 Unit)
Cohomology theories and operations, homotopy and obstruction theory, and CW complexes; spectral sequences. Multiple registrations allowed.

MATH 465-3 Algebraic Topology II (1 Unit)
Cohomology theories and operations, homotopy and obstruction theory, and CW complexes; spectral sequences. Multiple registrations allowed.

MATH 468-0 Homological Algebra (1 Unit)
Exact sequences, Ext and Tor, and homological dimensions.

MATH 470-1 Algebra (1 Unit)

MATH 470-2 Algebra (1 Unit)

MATH 470-3 Algebra (1 Unit)

MATH 477-0 Commutative Algebra (1 Unit)
Research in commutative algebra: theory of depth (regular sequences, Koszul complexes), dimension theory, completions, Hilbert functions, Cohen-Macaulay modules, excellent rings, Hensel rings, and minimal resolutions. Prerequisites: MATH 470-1, MATH 470-2, MATH 470-3 or equivalent.

MATH 478-0 Representation Theory (1 Unit)
Topics in the representation theory and cohomology of finite and infinite groups, including compact and non-compact Lie groups.

MATH 482-1 Algebraic Number Theory (1 Unit)
The theory of global and local fields; various special topics. 2. Abelian Galois extensions of algebraic number fields (class field theory). Complex multiplication, other examples, and relations with geometry.

MATH 482-2 Algebraic Number Theory (1 Unit)
Abelian Galois extensions of algebraic number fields (class field theory). Complex multiplication, other examples, and relations with geometry.

MATH 483-1 Algebraic Geometry (1 Unit)
Introduction to classical and scheme theoretic methods of algebraic geometry. Algebraic vector bundles, sheaf cohomology, the Riemann-Roch theorem for curves, and intersection theory.

MATH 483-2 Algebraic Geometry (1 Unit)
Introduction to classical and scheme theoretic methods of algebraic geometry. Algebraic vector bundles, sheaf cohomology, the Riemann-Roch theorem for curves, and intersection theory.

MATH 483-3 Algebraic Geometry (1 Unit)
Introduction to classical and scheme theoretic methods of algebraic geometry. Algebraic vector bundles, sheaf cohomology, the Riemann-Roch theorem for curves, and intersection theory.

MATH 484-0 Lie Theory (1 Unit)
Topics in the theory of Lie algebras and Lie groups including classification.

MATH 485-1 Modular Forms (1 Unit)
Introduction to the theory of modular forms. Congruence subgroups of SL(2,\Z), the definitions of modular functions and modular forms, Fourier expansions, Hecke operators, theta functions, modular curves.

**MATH 486-1 Algebraic K-Theory (1 Unit)**
Classical algebraic K-theory. Functors \(K_0\) and \(K_1\); origins in and relations with topology; congruence subgroup problem; techniques of computation: exact sequences, localization, resolution, and devissage; polynomial and related extensions; higher K-theories: Karoubi-Villamayor, Quillen.

**MATH 486-2 Algebraic K-Theory (1 Unit)**
Classical algebraic K-theory. Functors \(K_0\) and \(K_1\); origins in and relations with topology; congruence subgroup problem; techniques of computation: exact sequences, localization, resolution, and devissage; polynomial and related extensions; higher K-theories: Karoubi-Villamayor, Quillen.

**MATH 486-3 Algebraic K-Theory (1 Unit)**
Classical algebraic K-theory. Functors \(K_0\) and \(K_1\); origins in and relations with topology; congruence subgroup problem; techniques of computation: exact sequences, localization, resolution, and devissage; polynomial and related extensions; higher K-theories: Karoubi-Villamayor, Quillen.

**MATH 495-0 Statistical Phenomena in the Theory of Networks (1 Unit)**
This interdisciplinary course combines graph theory and probability theory to develop a rigorous foundation for the study of network-related problems.

**MATH 499-0 Independent Study (1 Unit)**
Permission of instructor and department required. May be repeated for credit.

**MATH 511-1 Topics in Analysis (1 Unit)**
Topics in Analysis and Probability Theory.

**MATH 511-2 Topics in Analysis (1 Unit)**
Topics in Analysis and Probability Theory.

**MATH 511-3 Topics in Analysis (1 Unit)**
Topics in Analysis and Probability Theory.

**MATH 512-1 Topics in Partial Differential Equations (1 Unit)**
Topics in Partial Differential Equations.

**MATH 512-2 Topics in Partial Differential Equations (1 Unit)**
Topics in Partial Differential Equations.

**MATH 512-3 Topics in Partial Differential Equations (1 Unit)**
Topics in Partial Differential Equations.

**MATH 513-1 Topics in Dynamical Systems (1 Unit)**
Topics in Partial Differential Equations.

**MATH 513-2 Topics in Dynamical Systems (1 Unit)**
Topics in Partial Differential Equations.

**MATH 513-3 Topics in Dynamical Systems (1 Unit)**
Topics in Partial Differential Equations.

**MATH 514-1 Topics in Geometry (1 Unit)**
Topics in Geometry.

**MATH 514-2 Topics in Geometry (1 Unit)**
Topics in Geometry.

**MATH 514-3 Topics in Geometry (1 Unit)**
Topics in Geometry.

**MATH 515-1 Topics in Geometry and Topology (1 Unit)**
This is a working seminar for students with interests in geometry, topology, and related fields. Its primary aim is to introduce students to research subjects of current interest to faculty members in these areas.

**MATH 515-2 Topics in Geometry and Topology (1 Unit)**
This is a working seminar for students with interests in geometry, topology, and related fields. Its primary aim is to introduce students to research subjects of current interest to faculty members in these areas.

**MATH 515-3 Topics in Geometry and Topology (1 Unit)**
This is a working seminar for students with interests in geometry, topology, and related fields. Its primary aim is to introduce students to research subjects of current interest to faculty members in these areas.

**MATH 516-1 Topics in Topology (1 Unit)**
Topics in Topology.

**MATH 517-1 Topics in Algebra (1 Unit)**
Topics in Algebra.

**MATH 517-2 Topics in Algebra (1 Unit)**
Topics in Algebra.

**MATH 517-3 Topics in Algebra (1 Unit)**
Topics in Algebra.

**MATH 518-1 Topics in Number Theory (1 Unit)**
Topics in Number Theory.

**MATH 518-2 Topics in Number Theory (1 Unit)**
Topics in Number Theory.

**MATH 518-3 Topics in Number Theory (1 Unit)**
Topics in Number Theory.

**MATH 519-0 Responsible Conduct of Research Training (0 Unit)**
Responsible Conduct of Research Training.

**MATH 520-1 Topics in Mathematical Physics (1 Unit)**
Topics in Mathematical Physics.

**MATH 521-1 Topics in Representation Theory (1 Unit)**
Topics in Representation Theory.

**MATH 521-2 Topics in Representation Theory (1 Unit)**
Topics in Representation Theory.

**MATH 521-3 Topics in Representation Theory (1 Unit)**
Topics in Representation Theory.

**MATH 580-0 Seminar in College Teaching (0 Unit)**
A weekly two-hour seminar introducing the technique, philosophy, and practice of teaching undergraduate mathematics. Student presentations are critiqued by fellow students, as well as a senior faculty member.

**MATH 590-0 Research (1-3 Units)**
SEE DEPT FOR SECTION AND PERMISSION NUMBERS - Independent investigation of selected problems pertaining to thesis or dissertation. May be repeated for credit.